

## Discrete Mathematics Quiz 2

Name: \_\_\_\_\_

NYU Net ID: \_\_\_\_\_

Generate multiple quizzes; for each quiz, select a single #1 question, a single #2, a single #3, and a single #4. Since this is  $3 * 2 * 2 * 3$  choices, that gives us 36 possible quizzes.

1.1)  $p \vee (p \wedge q) \equiv$

a)  $q$

b)  $\neg q$

\*c)  $p$

d)  $\neg p$

1.2)  $\neg(p \vee q) \equiv$

\*a)  $\neg p \wedge \neg q$

b)  $\neg p \wedge q$

c)  $p \wedge \neg q$

d)  $\neg p \vee \neg q$

1.3)  $p \wedge (p \vee q) \equiv$

a)  $\neg p$

b)  $\neg q$

c)  $q$

\*d)  $p$

2.1) If the domain of  $x$  is all integers, is  $\forall x (x^2 > 0)$

a) True

\*b) False

2.2) If the domain of  $x$  is all integers, is  $\forall x (x^3 > 0)$

a) True

\*b) False

3.1) If  $E(x)$  means "x is even" and  $P(x)$  means "x is prime", then  $\forall x (P(x) \rightarrow E(x))$  is

a) True

\*b) False

3.2) If  $O(x)$  means "x is odd", then  $\forall x (O(x) \rightarrow O(x^2))$  is

\*a) True

b) False

4.1) Let  $L(a, b, c)$  be the statement "a loves b at time c," where the domain for both a and b consists of all living people in the world and time t consists of all moments from the year 1900 to 2018. Translate "Everybody loves somebody sometime" into a quantified logical statement.

Answer like " $\forall x \exists y \exists t (L(x, y, t))$ "

4.2) Let  $S(a, b)$  be the statement "a has sent an e-mail message to b," where the domain for both a and b consists of all students in your class. Translate "Every student in your class HAS BEEN SENT a message from at least one student in your class." into a quantified logical statement.

Answer like " $\forall x \exists y (S(y, x))$ "

4.3) Let  $C(x)$  is "x is a comedian" and  $F(x)$  is "x is funny" and the domain consists of all people. Translate "Every comedian is funny." into predicate logic.

Answer like " $\forall x (C(x) \rightarrow F(x))$ "